Clustering: Grouping Related Docs



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Motivating clustering approaches

Goal: Structure documents by topic

Discover groups (*clusters*) of related articles



Why might clustering be useful?



Learn user preferences

Set of clustered documents read by user



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Clustering: An unsupervised learning task

What if some of the labels are known?

Training set of labeled docs



Multiclass classification problem



Example of supervised learning

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Clustering

No labels provided ...uncover cluster structure from input alone

Input: docs as vectors **x**_i **Output:** cluster labels z_i

> An **unsupervised learning** task



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What defines a cluster?

Cluster defined by center & shape/spread

Assign observation \mathbf{x}_i (doc) to cluster k (topic label) if

- Score under cluster k is higher than under others
- For simplicity, often define score as distance to cluster center (ignoring shape)



Hope for unsupervised learning

Easy

Impossible





Other (challenging!) clusters to discover...



Other (challenging!) clusters to discover...



k-means: A clustering algorithm

k-means

Assume

-Score= distance to cluster center (smaller better)



0. Initialize cluster centers

 μ_1,μ_2,\ldots,μ_k



- 0. Initialize cluster centers
- 1. Assign observations to closest cluster center



Voronoi tesselation (for visualization only... you don't heed to compute this)

- 0. Initialize cluster centers
- 1. Assign observations to closest cluster center
- 2. Revise cluster centers as mean of assigned observations

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 \mathbf{X}_i

- 0. Initialize cluster centers
- 1. Assign observations to closest cluster center
- 2. Revise cluster centers as mean of assigned observations
- 3. Repeat 1.+2. until convergence



k-means as coordinate descent

A coordinate descent algorithm

1. Assign observations to closest cluster center

$$z_i \leftarrow \arg\min_j ||\mu_j - \mathbf{x}_i||_2^2$$

2. Revise cluster centers as mean of assigned observations



A coordinate descent algorithm

1. Assign observations to closest cluster center

$$z_i \leftarrow \arg\min_j ||\mu_j - \mathbf{x}_i||_2^2$$

2. Revise cluster centers as mean of assigned observations

$$\mu_j \leftarrow \arg\min_{\mu} \sum_{i:z_i=j} ||\mu - \mathbf{x}_i||_2^2$$

A coordinate descent algorithm

1. Assign observations to closest cluster center

$$z_i \leftarrow \arg\min_j ||\mu_j - \mathbf{x}_i||_2^2$$

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$$\mu_j \leftarrow \arg\min_{\mu} \sum_{i:z_i=j} ||\mu - \mathbf{x}_i||_2^2$$

Alternating minimization 1. (z given μ) and 2. (μ given z) = coordinate descent

Convergence of k-means

Converges to:



- Local optimum



Convergence of k-means to local mode



Convergence of k-means to local mode



Convergence of k-means to local mode



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Smart initialization with k-means++

k-means++ overview

Initialization of k-means algorithm is critical to quality of local optima found

Smart initialization:

- 1. Choose first cluster center uniformly at random from data points
- 2. For each obs **x**, compute distance d(**x**) to nearest cluster center
- 3. Choose new cluster center from amongst data points, with probability of \mathbf{x} being chosen proportional to $d(\mathbf{x})^2$
- 4. Repeat Steps 2 and 3 until k centers have been chosen









k-means++ pros/cons

Computationally costly relative to random initialization, but the subsequent k-means often converges more rapidly

Tends to improve quality of local optimum and lower runtime

Assessing quality of the clustering and choosing the # of clusters

Which clustering do I prefer?



k-means objective





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What happens as k increases?

Can refine clusters more and more to the data

 \rightarrow overfitting!

1 # of observations Extreme case of k=N:

- can set each cluster center equal to datapoint
 heterogeneity =) ! (all distances to centers are)

Lowest possible cluster heterogeneity decreases with increasing k



MapReduce

Counting words on a single processor

(The "Hello World!" of MapReduce)

Suppose you have <u>10B</u> documents and <u>1 machine</u> and want to count the # of occurrences of each word in the corpus

Code:

Naïve parallel word counting

- Word counts are independent across documents (data parallel)
- Count occurrences in sets of documents separately, then merge



How do we do this for all words in vocab?

Back to sequential problem to merge counts...



Counting words in parallel & merging tables in parallel

Generate pairs (word,count) in parallel
 Merge counts for each word in parallel



Which words go to machine i? $h: V \rightarrow [1, 2, ..., # machines]$ Send counts of llearning' to machine h['learning']

How to map words to machines? Use a hash function!

h(word index) \rightarrow machine index

MapReduce abstraction



MapReduce has long history in functional programming

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Popularized by Google, and subsequently by open-source Hadoop implementation from Yahoo!
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MapReduce – Execution overview



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Improving performance: Combiners

• Naïve implementation of MapReduce is very wasteful in communication during shuffle:



- Combiner: Simple solution...Perform reduce locally before communicating for global reduce
 - Works because reduce is commutative-associative



Scaling up k-means via MapReduce

MapReducing 1 iteration of k-means

Classify: Assign observations to closest cluster center

$$z_i \leftarrow \arg\min_j ||\mu_j - \mathbf{x}_i||_2^2$$

Map: For each data point, given $({\mu_i}, \mathbf{x}_i)$, emit (z_i, \mathbf{x}_i)

Recenter: Revise cluster centers as mean of assigned observations

$$\mu_j = \frac{1}{n_j} \sum_{i: z_i = k} \mathbf{x}_i$$

Reduce: Average over all points in cluster j ($z_i = k$)

Classification step as Map

Classify: Assign observations to closest cluster center

$$z_{i} \leftarrow \arg\min_{j} ||\mu_{j} - \mathbf{x}_{i}||_{2}^{2}$$

$$\max \left[[\mu_{1}, \mu_{2}, ..., \mu_{k}], \mathbf{x}_{i} \right]$$

$$z_{i} \leftarrow \arg\min_{j} ||\mu_{j} - \mathbf{x}_{i}||_{2}^{2}$$

$$\operatorname{emit}(z_{i}, \mathbf{x}_{i})$$

$$datapoint$$

$$cluster label$$

$$e.g. \operatorname{emit}(2, [17, 0, 1, 7, 0, 0, 5])$$

Recenter step as Reduce

Recenter: Revise cluster centers as mean of assigned observations

 $\mu_j = \frac{1}{n_j} \sum_{i:z_i = k} \mathbf{x}_i$ cluster lat reduce(j, x_in_clusterj : [x₁, x₃,...,]) sum = 0 « total mass in cluster Count = 0 - total # of obs. in cluster for **x** in x_in_clusterj sum += xcount += 1emit(j, sum/count)

Some practical considerations

k-means needs an iterative version of MapReduce

Not standard formulation

Mapper needs to get data point and all centers

- A lot of data!
- Better implementation: mapper gets many data points

Summary of parallel k-means using MapReduce

Map: classification step; data parallel over data points

Reduce: recompute means; data parallel over centers

Other examples

Clustering images

- For search, group as:
 - Ocean
 - Pink flower
 - Dog

. . .

- Sunset
- Clouds







Structuring web search results

- Search terms can have multiple meanings
- Example: "cardinal"



• Use clustering to structure output

Grouping patients by medical condition

 Better characterize subpopulations and diseases

Example: Patients and seizures are diverse











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Cluster seizures by observed time courses



Products on Amazon

• Discover product categories from purchase histories



• Or discovering groups of **users**

Discovering similar neighborhoods

- Task 1: Estimate price at a small regional level
- Challenge:
 - Only a few (or no!) sales
 in each region per month
- Solution:
 - Cluster regions with similar trends and share information within a cluster



Discovering similar neighborhoods

- Task 2: Forecast violent crimes to better task police
- Again, cluster regions and share information!
- Leads to improved predictions compared to examining each region independently

Washington, DC

Summary for k-means and MapReduce

What you can do now...

- Describe potential applications of clustering
- Describe the input (unlabeled observations) and output (labels) of a clustering algorithm
- Determine whether a task is supervised or unsupervised
- Cluster documents using k-means
- Interpret k-means as a coordinate descent algorithm
- Define data parallel problems
- Explain Map and Reduce steps of MapReduce framework
- Use existing MapReduce implementations to parallelize kmeans, understanding what's being done under the hood