

Emily Fox & Carlos Guestrin Machine Learning Specialization University of Washington

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#### Predicting potential loan defaults

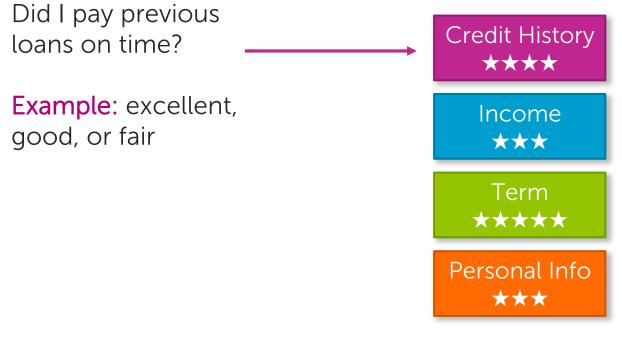
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# What makes a loan risky?



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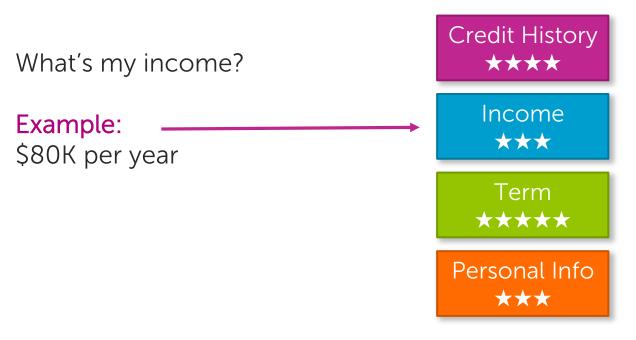
# Credit history explained



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#### Income



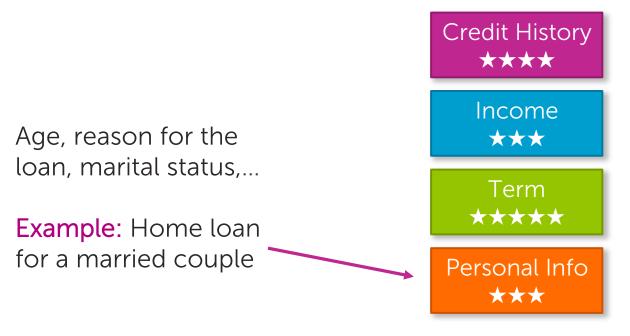
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#### Loan terms



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## **Personal information**

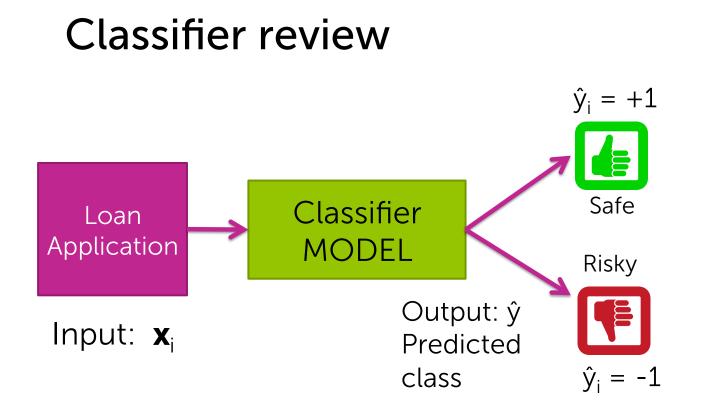


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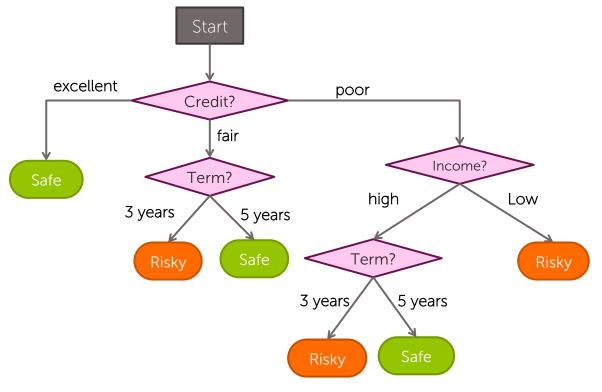
### Intelligent application



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## This module ... decision trees

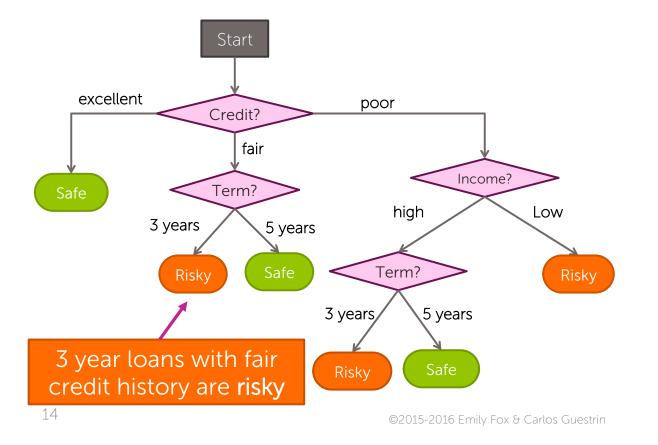


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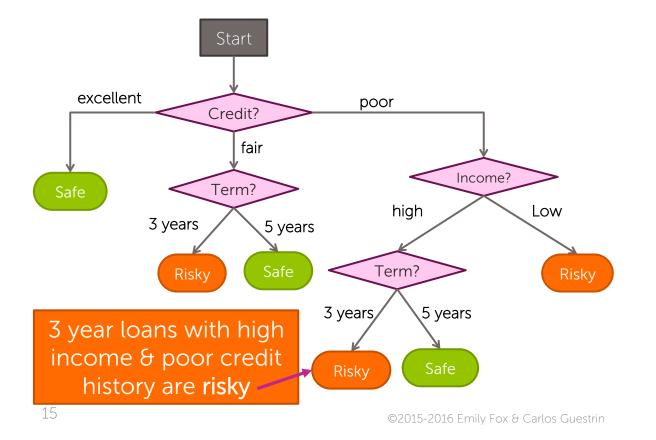
#### Decision trees: Intuition

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## What does a decision tree represent?

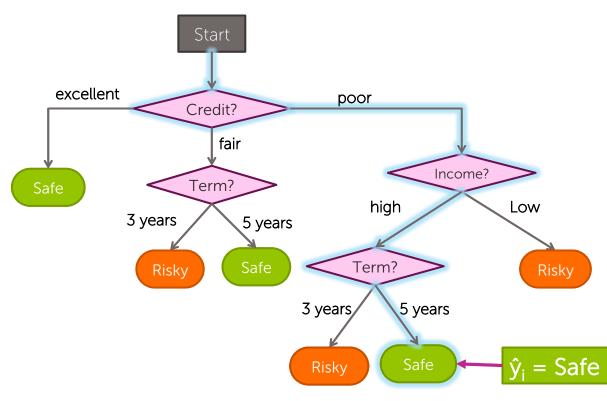


## What does a decision tree represent?



# Scoring a loan application

 $\mathbf{x}_{i} =$ (Credit = poor, Income = high, Term = 5 years)

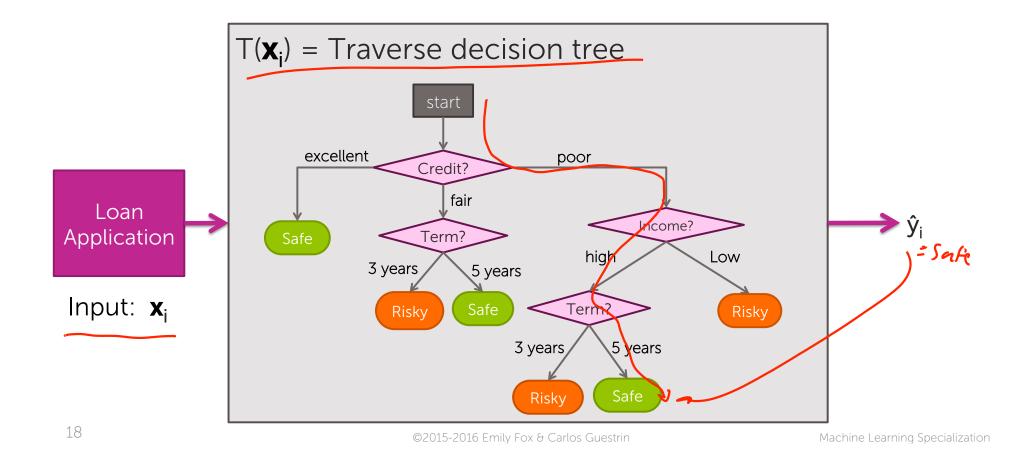


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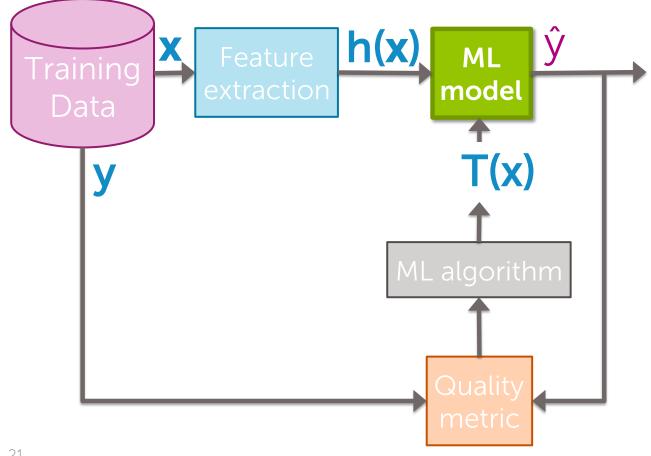
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#### Decision tree model



#### Decision tree learning task

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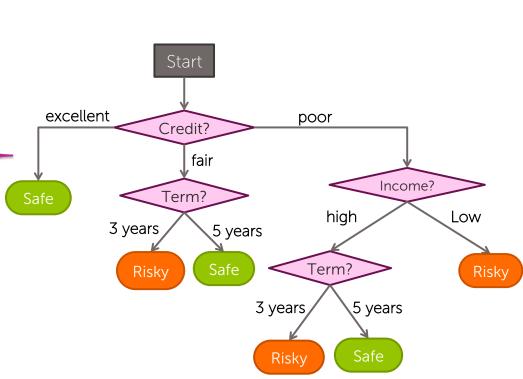
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#### Learn decision tree from data?

K.(X)	らっとう	$h_3(x)$	Lorg
Credit	Term	Income	У
excellent	3 yrs	high	safe
fair	5 yrs	low	risky
fair	3 yrs	high	safe
poor	5 yrs	high	risky
excellent	3 yrs	low	risky
fair	5 yrs	low	safe
poor	3 yrs	high	risky
poor	5 yrs	low	safe
fair	3 yrs	high	safe

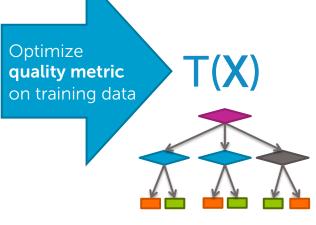


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# Decision tree learning problem

#### Training data: N observations $(\mathbf{x}_i, y_i)$

Credit	Term	Income	у
excellent	3 yrs	high	safe
fair	5 yrs	low	risky
fair	3 yrs	high	safe
poor	5 yrs	high	risky
excellent	3 yrs	low	risky
fair	5 yrs	low	safe
poor	3 yrs	high	risky
poor	5 yrs	low	safe
fair	3 yrs	high	safe



#### Quality metric: Classification error

• Error measures fraction of mistakes

Error = <u># incorrect predictions</u> # examples

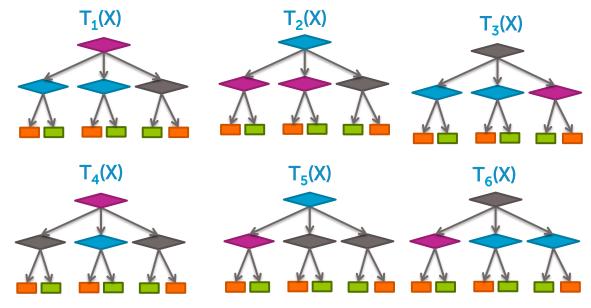
- Best possible value : 0.0
- Worst possible value: 1.0

#### Find the tree with lowest classification error

Credit	Term	Income	У
excellent	3 yrs	high	safe
fair	5 yrs	low	risky
fair	3 yrs	high	safe
poor	5 yrs	high	risky
excellent	3 yrs	low	risky
fair	5 yrs	low	safe
poor	3 yrs	high	risky
poor	5 yrs	low	safe
fair	3 yrs	high	safe

#### How do we find the best tree?

Exponentially large number of possible trees makes decision tree learning hard! (NP-hard problem)



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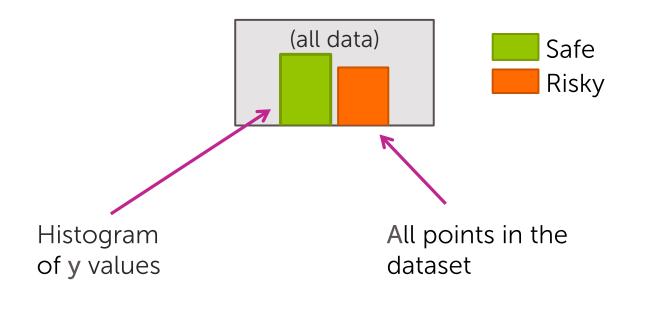
# Simple (greedy) algorithm finds "good" tree

Credit	Term	Income	у
excellent	3 yrs	high	safe
fair	5 yrs	low	risky
fair	3 yrs	high	safe
poor	5 yrs	high	risky
excellent	3 yrs	low	risky
fair	5 yrs	low	safe
poor	3 yrs	high	risky
poor	5 yrs	low	safe
fair	3 yrs	high	safe

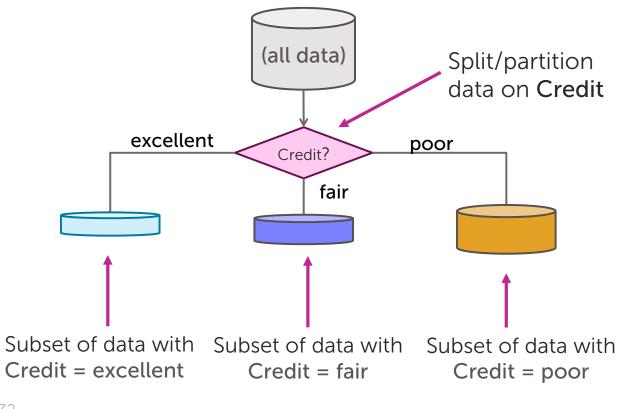
#### Greedy decision tree learning: Algorithm outline

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# Step 1: Start with an empty tree



## Step 2: Split on a feature

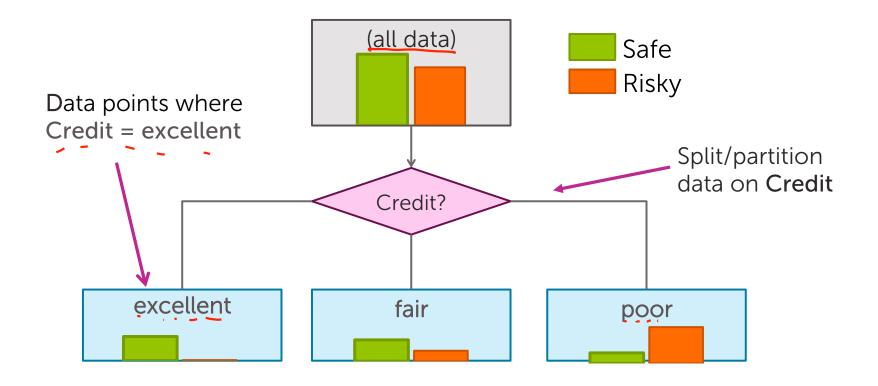


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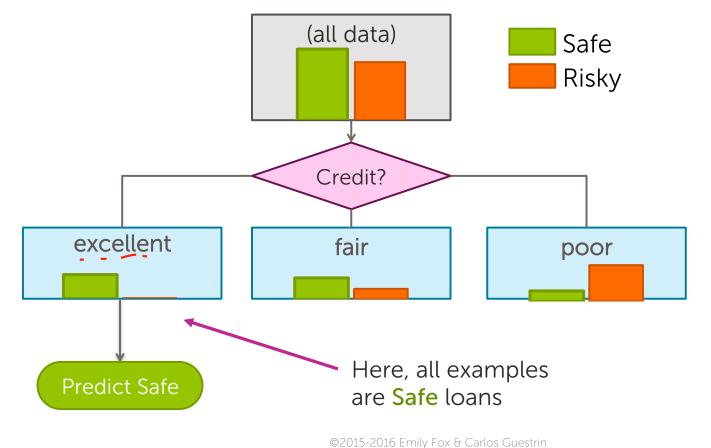
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## Feature split explained

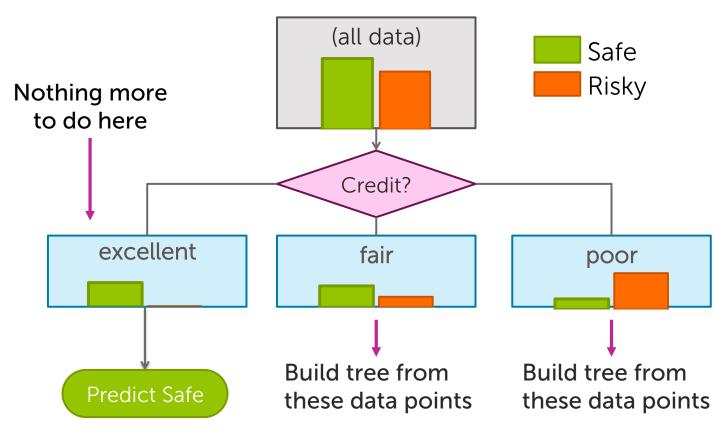


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# Step 3: Making predictions



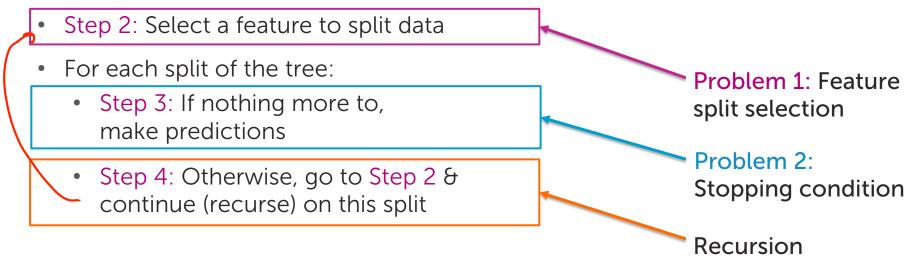
#### **Step 4: Recursion**



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# Greedy decision tree learning





#### Feature split learning

#### Decision stump learning

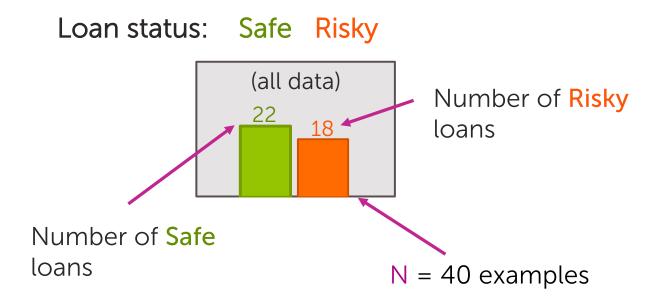
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## Start with the data

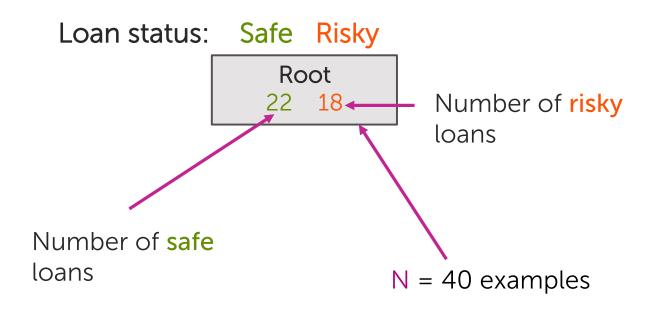
#### Assume N = 40, 3 features

Credit	Term	Income	у
excellent	3 yrs	high	safe
fair	5 yrs	low	risky
fair	3 yrs	high	safe
poor	5 yrs	high	risky
excellent	3 yrs	low	risky
fair	5 yrs	low	safe
poor	3 yrs	high	risky
poor	5 yrs	low	safe
fair	3 yrs	high	safe

## Start with all the data

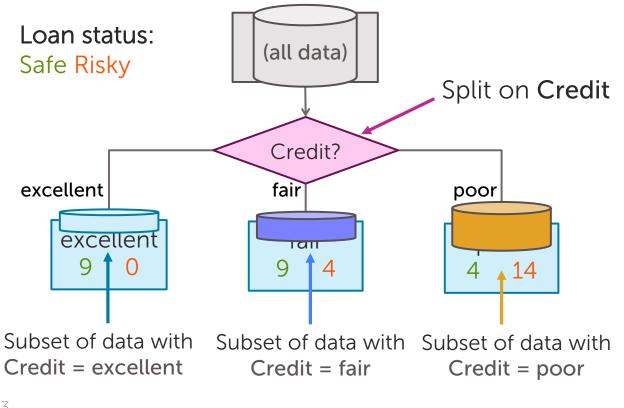


## Compact visual notation: Root node



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# Decision stump: Single level tree

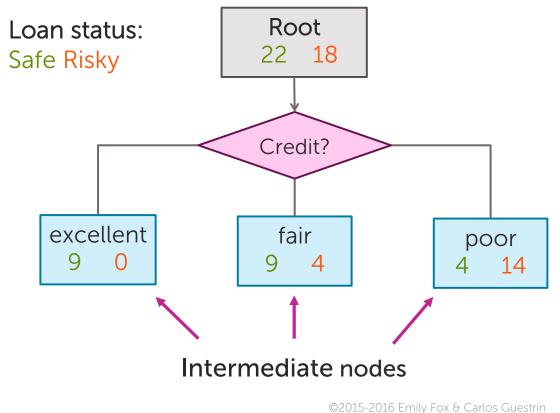


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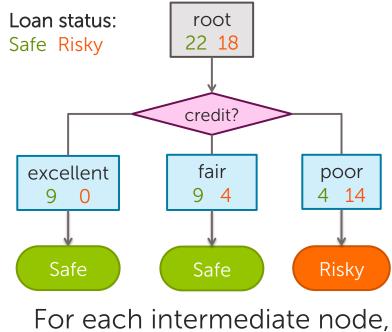
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## Visual Notation: Intermediate nodes



# Making predictions with a decision stump



set  $\hat{\mathbf{y}} = \mathbf{majority value}$ 

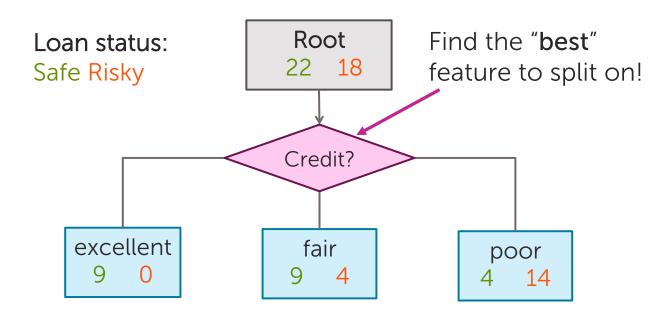
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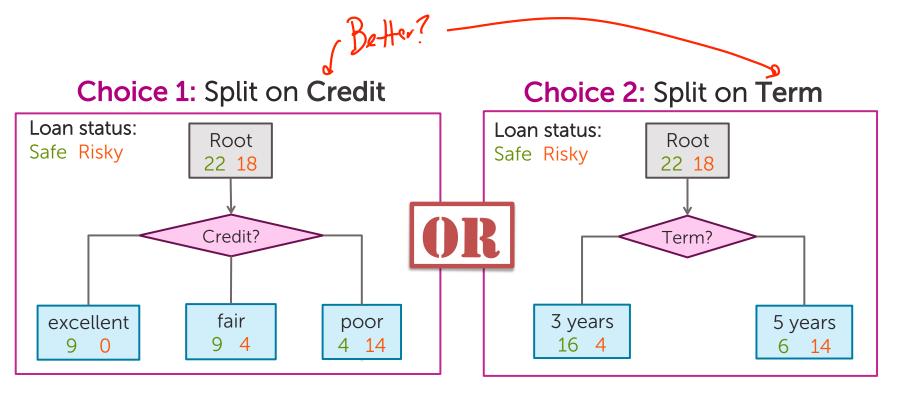
#### Selecting best feature to split on

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#### How do we learn a decision stump?

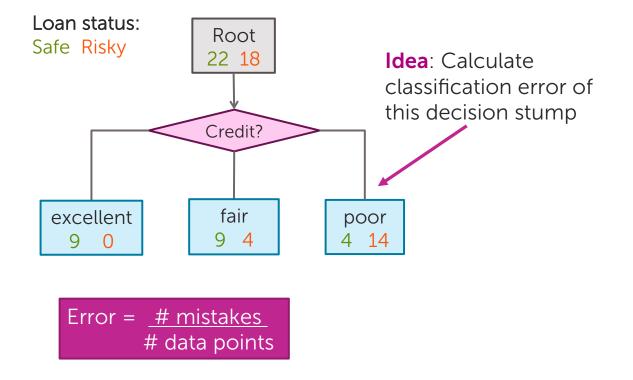


#### How do we select the best feature?



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# How do we measure effectiveness of a split?

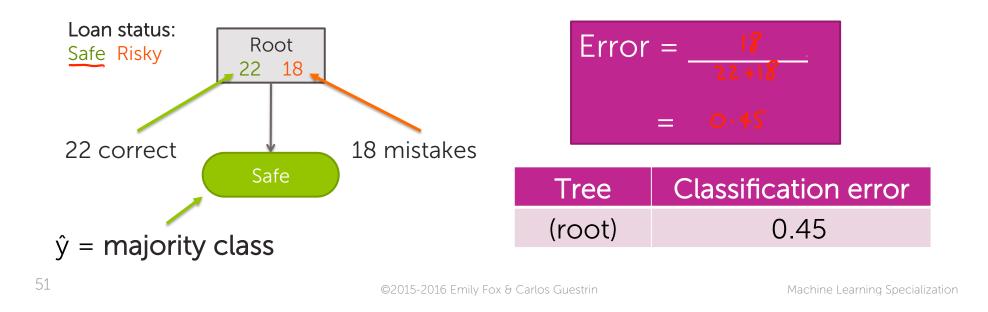


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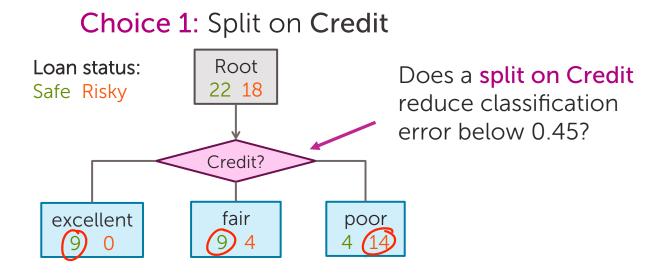
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#### Calculating classification error

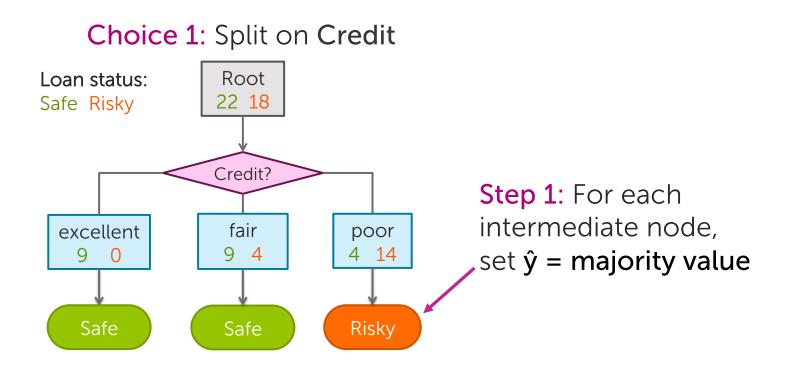
- Step 1: ŷ = class of majority of data in node
- Step 2: Calculate classification error of predicting ŷ for this data



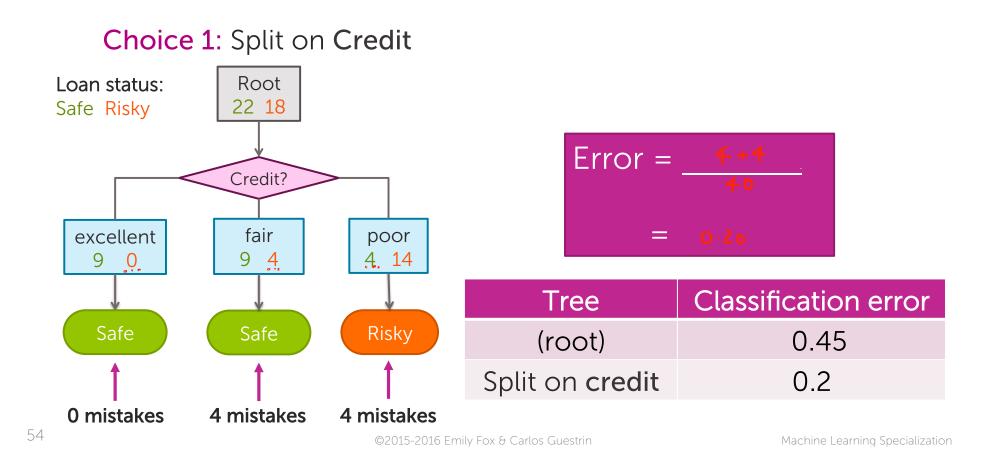
#### Choice 1: Split on credit history?



#### How good is the split on **Credit**?

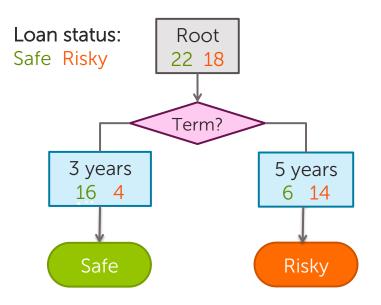


#### Split on Credit: Classification error



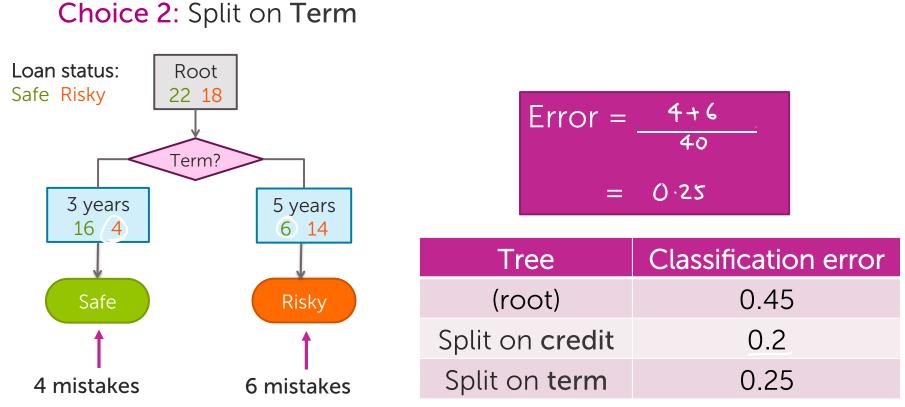
#### Choice 2: Split on Term?

Choice 2: Split on Term



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#### Evaluating the split on Term

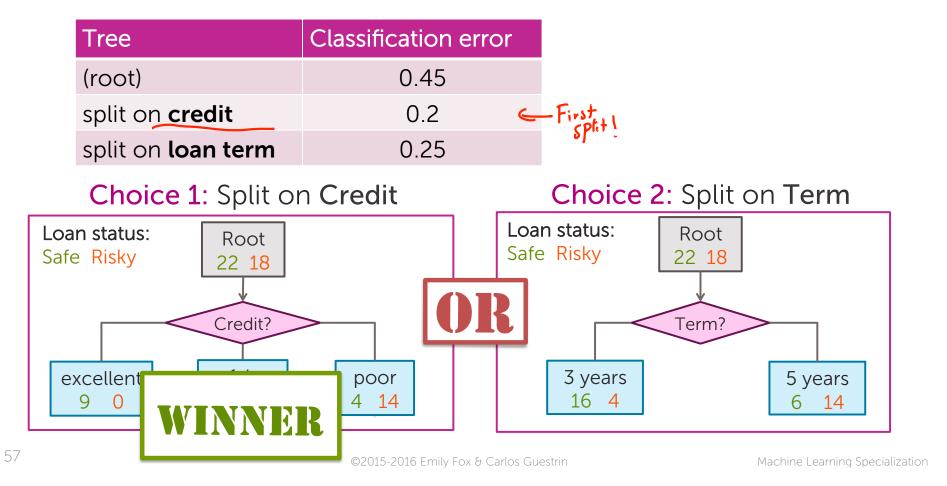


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#### Choice 1 vs Choice 2



#### Feature split selection algorithm

- Given a subset of data <u>M</u> (a node in a tree)
- For each feature  $h_i(\mathbf{x})$ :  $\boldsymbol{\epsilon}$  credit, two, income
  - 1. Split data of M according to feature h<sub>i</sub>(x)
  - 2. Compute classification error split
- Chose feature <a href="http://withlowest.classification.error">http://withlowest.classification.error</a>

#### Greedy decision tree learning

- Step 1: Start with an empty tree
- Step 2: Select a feature to split data
- For each split of the tree:
  - Step 3: If nothing more to, make predictions
  - Step 4: Otherwise, go to Step 2 & continue (recurse) on this split

Pick feature split leading to lowest classification error

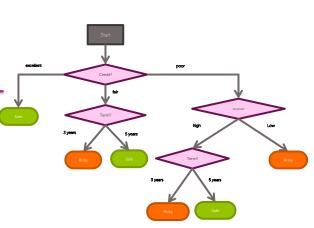
#### Decision Tree Learning: Recursion & Stopping conditions

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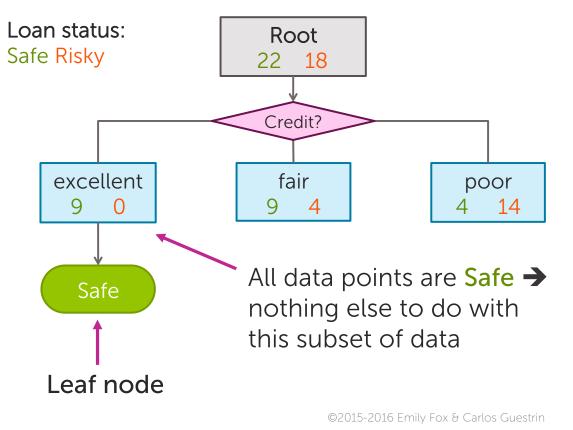
#### Learn decision tree from data?

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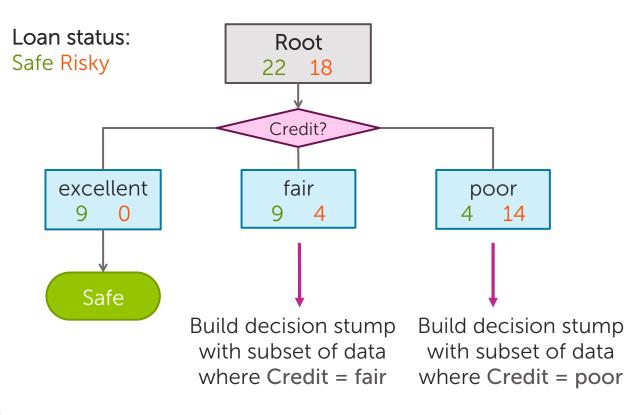
				. I
Credit	Term	Income	У	
excellent	3 yrs	high	safe	
fair	5 yrs	low	risky	
fair	3 yrs	high	safe	
poor	5 yrs	high	risky	
excellent	3 yrs	low	risky	
fair	5 yrs	low	safe	
poor	3 yrs	high	risky	
poor	5 yrs	low	safe	
fair	3 yrs	high	safe	



#### We've learned a decision stump, what next?

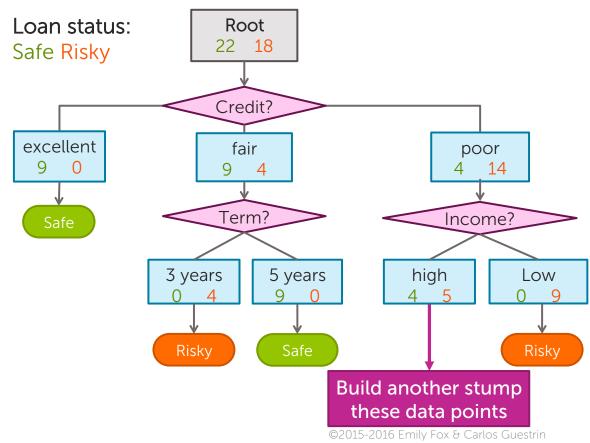


#### Tree learning = Recursive stump learning

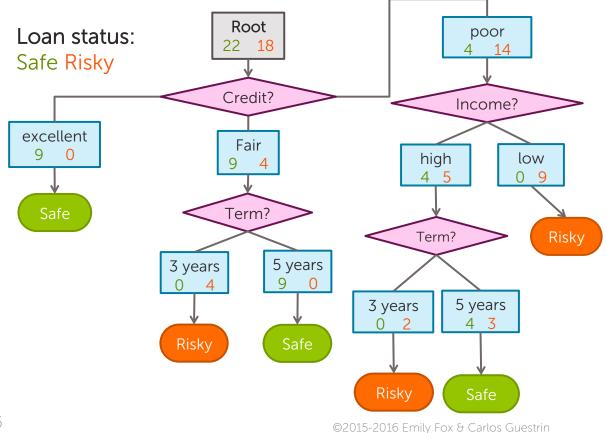


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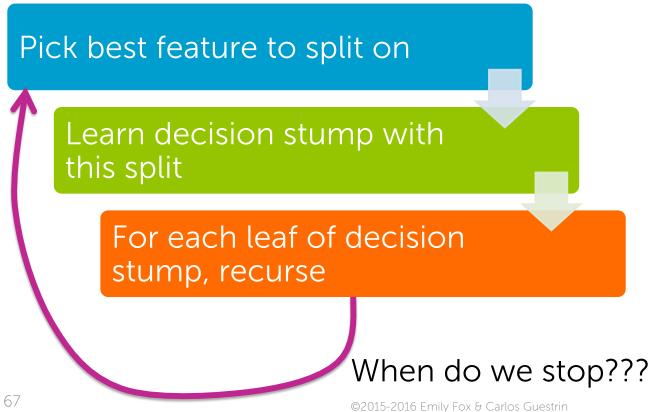
#### Second level



#### Final decision tree



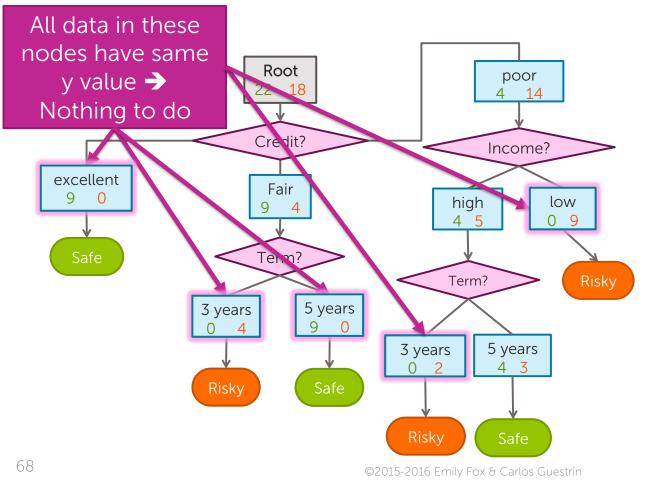
#### Simple greedy decision tree learning



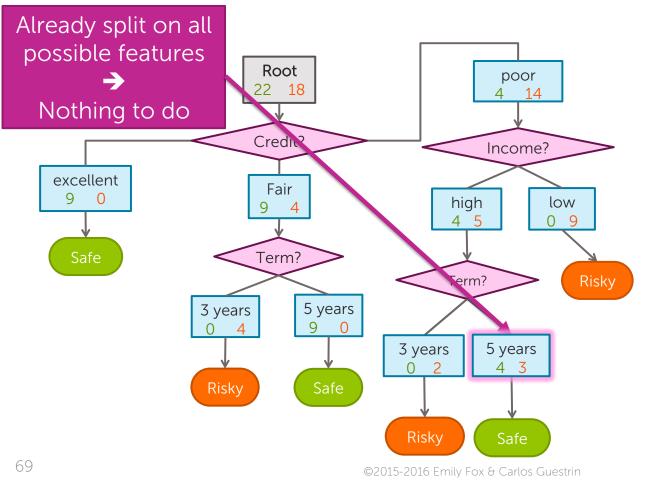
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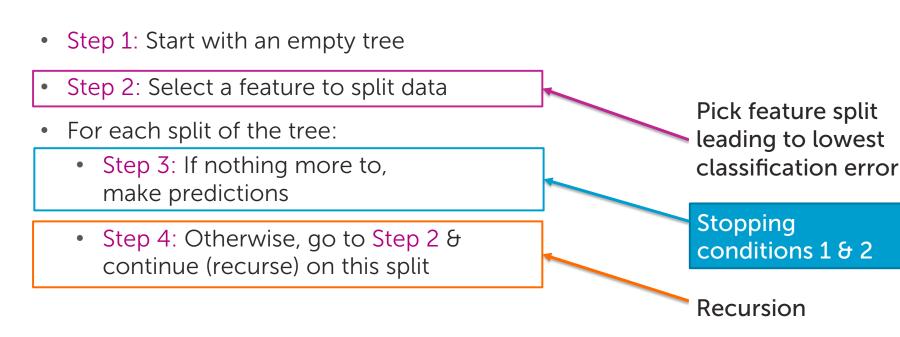
#### Stopping condition 1: All data agrees on y



#### Stopping condition 2: Already split on all features

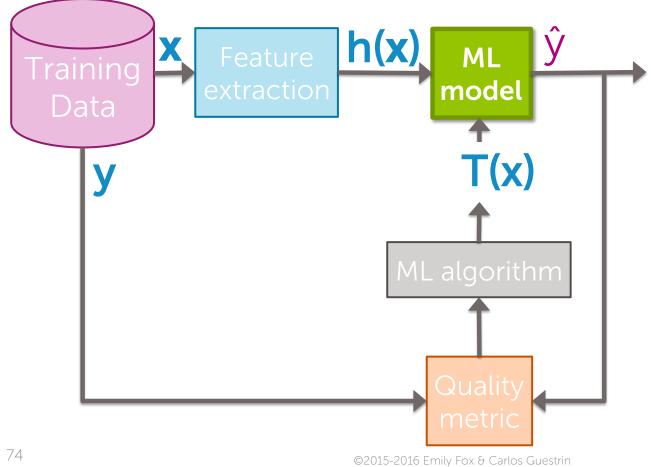


#### Greedy decision tree learning

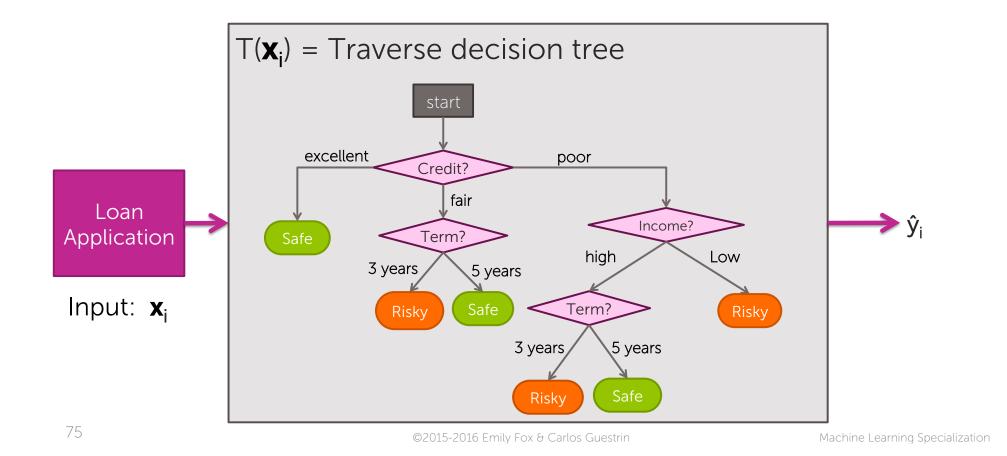


#### **Predictions with decision trees**

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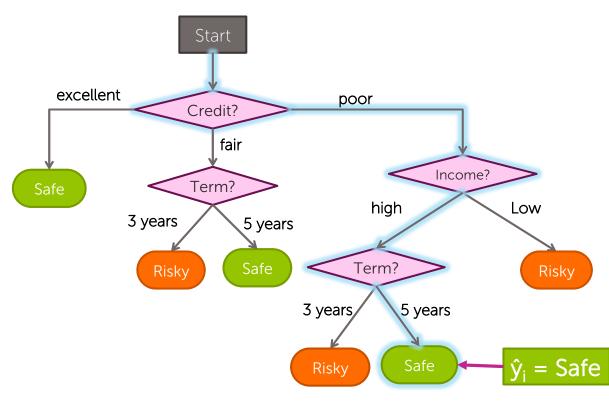


#### Decision tree model



### Traversing a decision tree

 $\mathbf{x}_{i} =$ (Credit = poor, Income = high, Term = 5 years)



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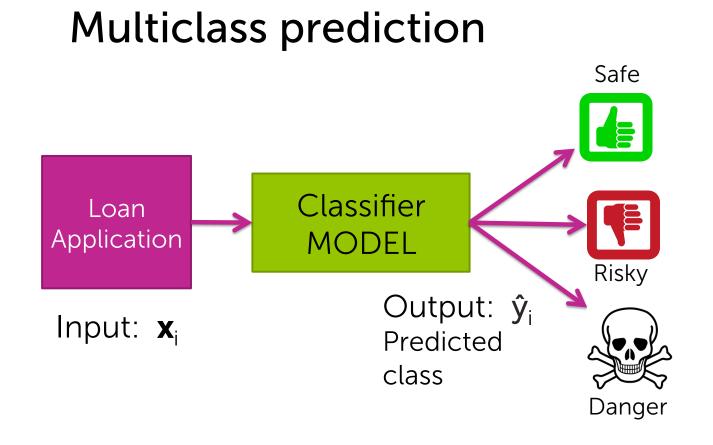
#### Decision tree prediction algorithm

#### predict(tree\_node, input)

- If current tree\_node is a leaf:
  - return majority class of data points in leaf
- else:
  - next\_note = child node of tree\_node whose feature value agrees with input
  - o return predict(next\_note, input)

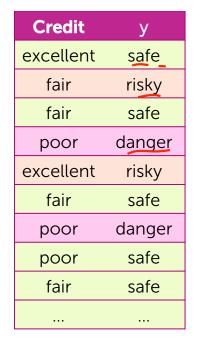
### Multiclass classification & predicting probabilities

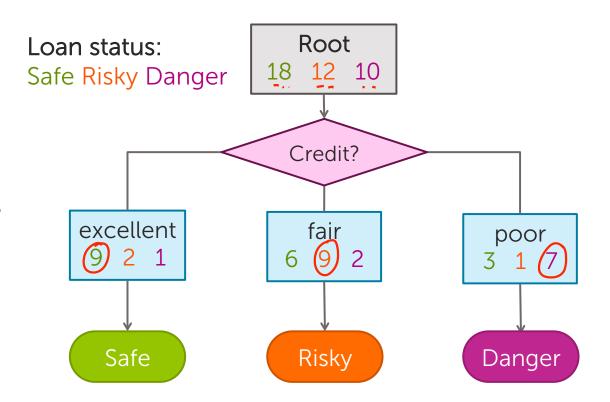
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#### Multiclass decision stump

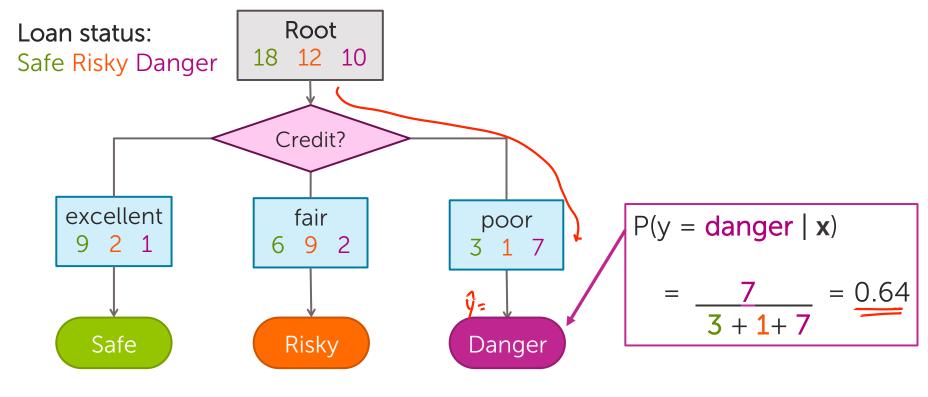
N = 40, 1 feature, 3 classes





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## Predicting probabilities with decision trees



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#### Decision tree learning: *Real valued features*

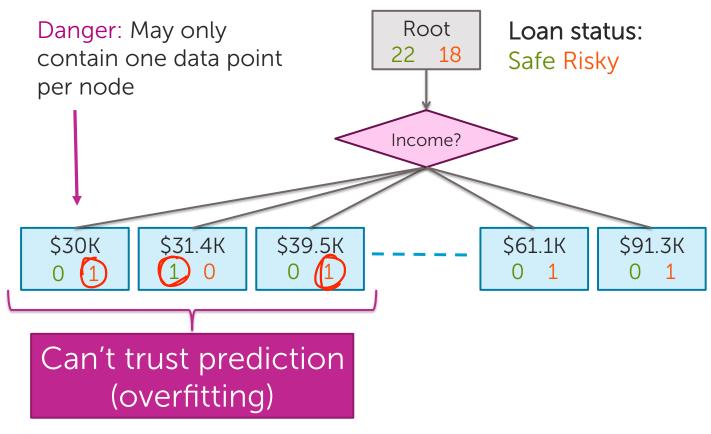
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#### How do we use real values inputs?

Income	Credit	Term	У
\$105 K	excellent	3 yrs	Safe
\$112 K	good	5 yrs	Risky
\$73 K	fair	3 yrs	Safe
\$69 K	excellent	5 yrs	Safe
\$217 K	excellent	3 yrs	Risky
\$120 K	good	5 yrs	Safe
\$64 K	fair	3 yrs	Risky
\$340 K	excellent	5 yrs	Safe
\$60 K	good	3 yrs	Risky

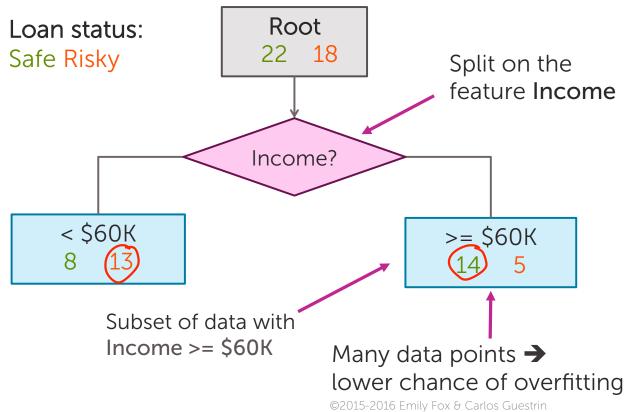
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#### Split on each numeric value?



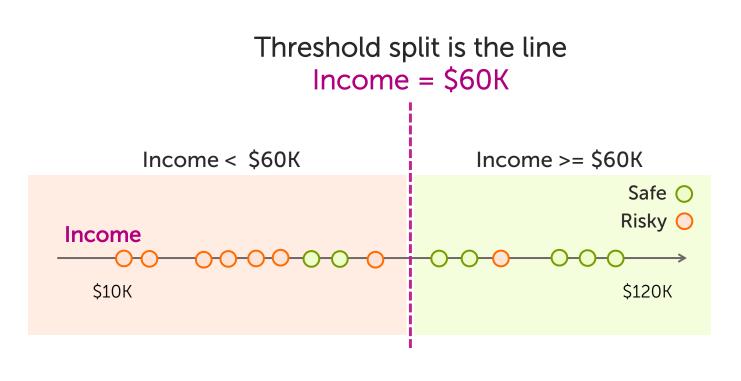
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# Alternative: Threshold split

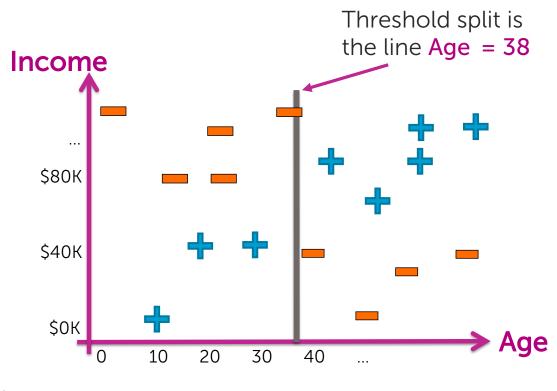


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## Threshold splits in 1-D



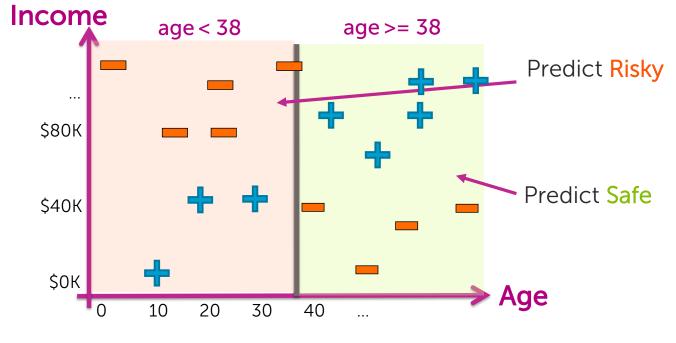
## Visualizing the threshold split



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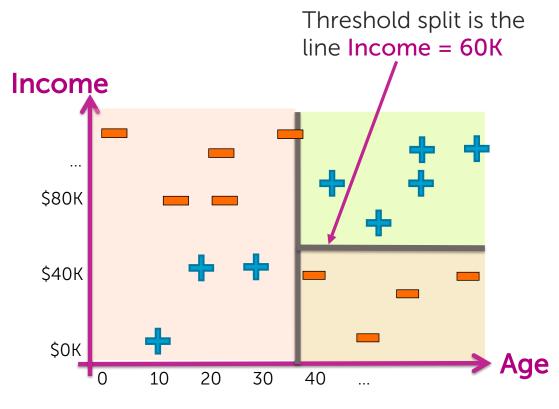
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# Split on Age >= 38



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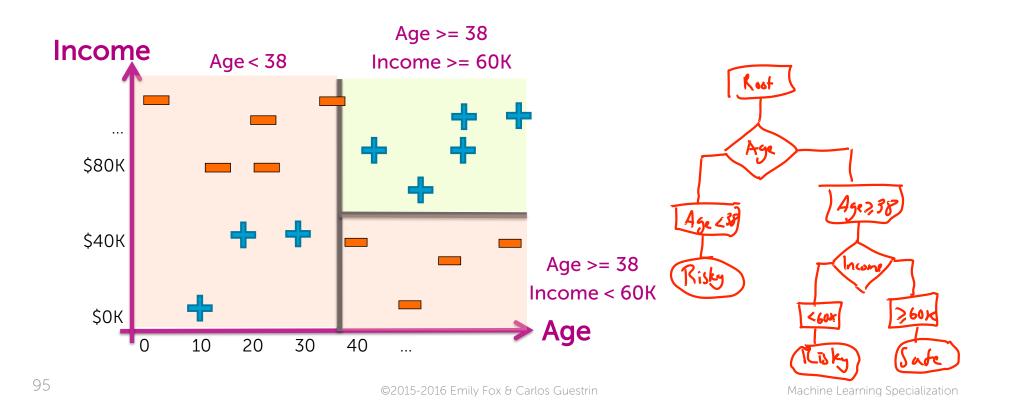
#### Depth 2: Split on Income >= \$60K



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# Each split partitions the 2-D space



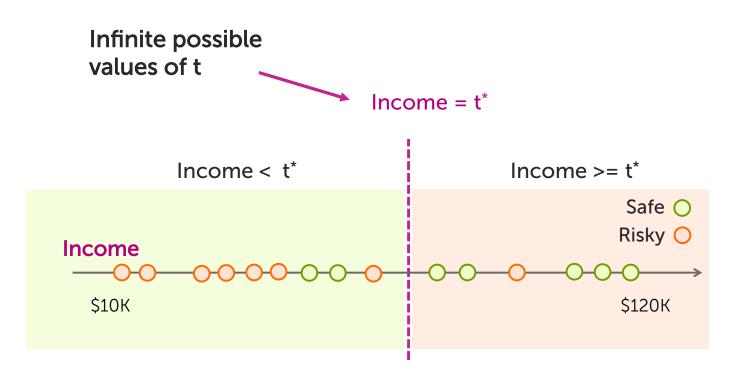


#### Finding the best threshold split

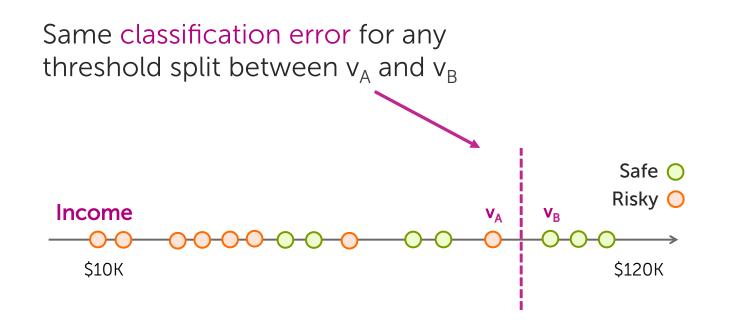


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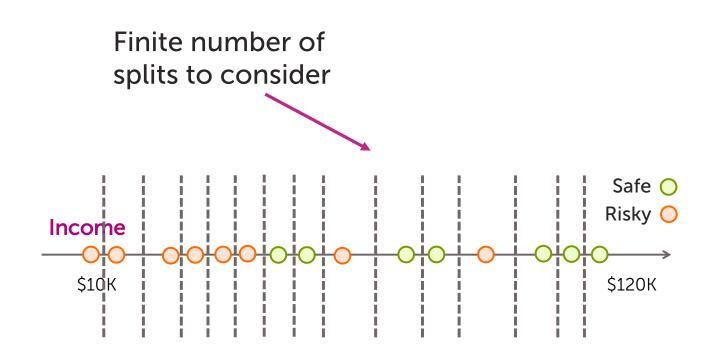
# Finding the best threshold split



#### Consider a threshold between points



#### Only need to consider mid-points



# Threshold split selection algorithm

Step 1: Sort the values of a feature h<sub>i</sub>(x) :

Let  $\{v_1, v_2, v_3, \dots v_N\}$  denote sorted values

• Step 2:

- Consider split  $t_i = (v_i + v_{i+1}) / 2$
- Compute classification error for treshold split h<sub>i</sub>(x) >= t<sub>i</sub>

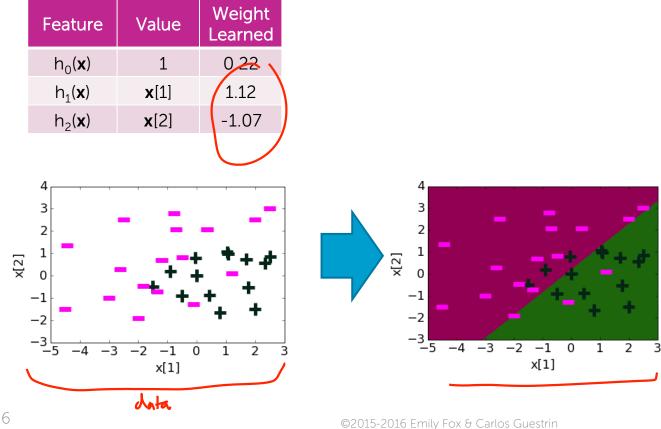
- Chose the t with the lowest classification error

Income

#### Decision trees vs logistic regression: Example

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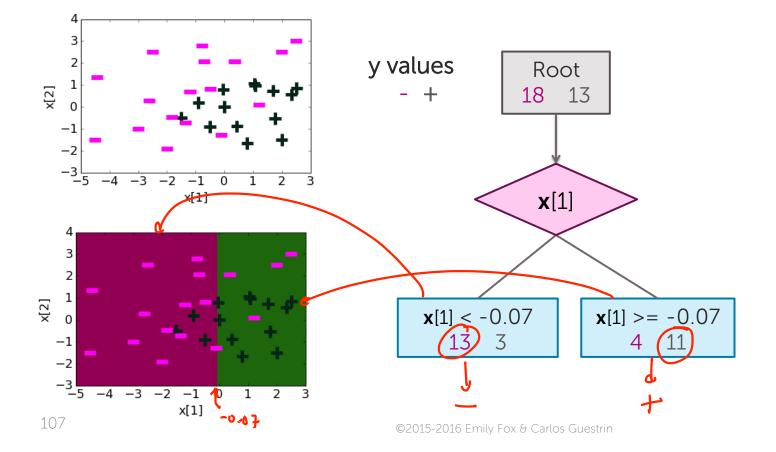
# Logistic regression



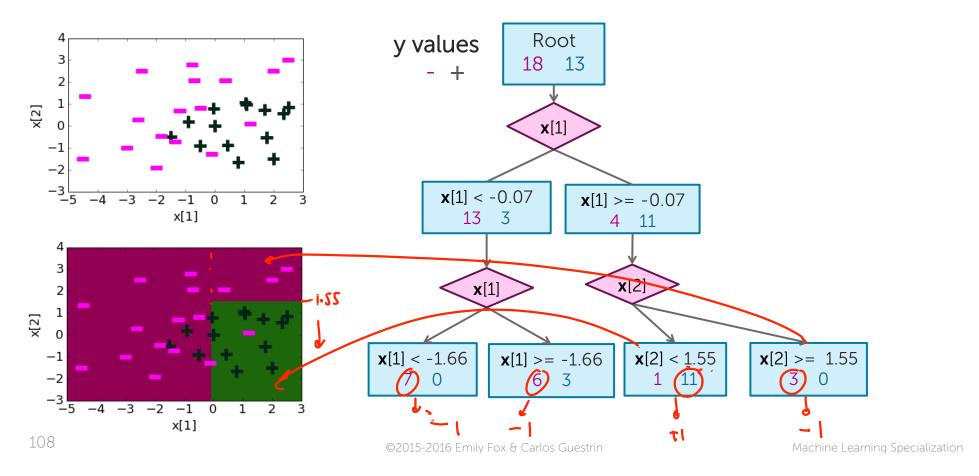
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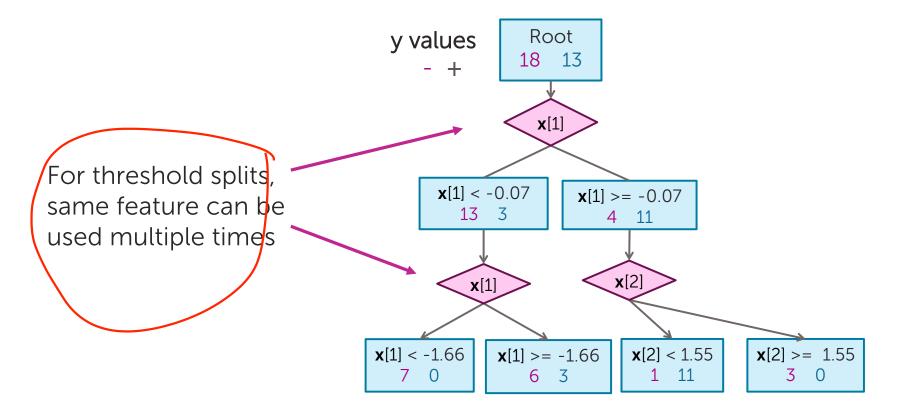




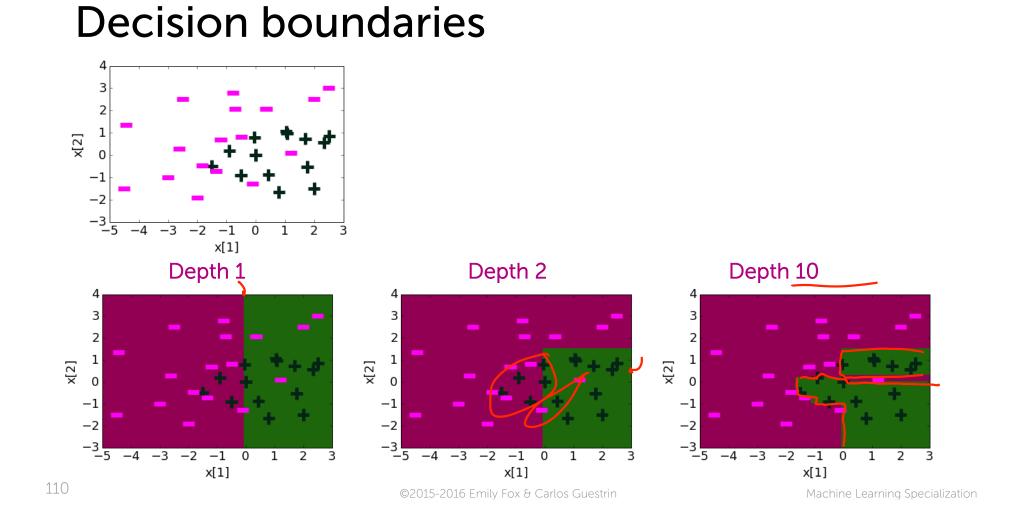




# Threshold split caveat



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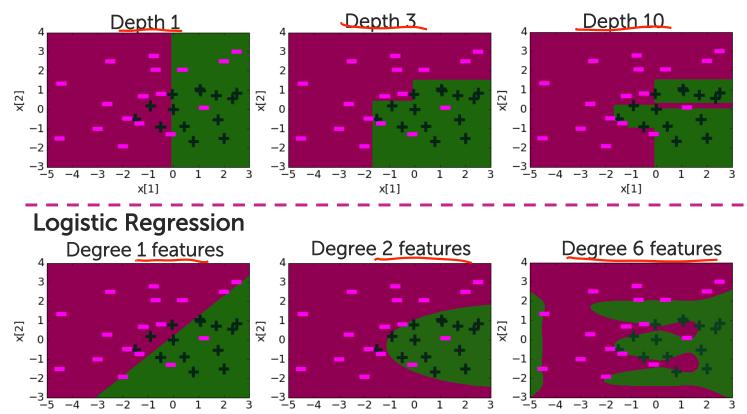


## **Comparing decision boundaries**

#### **Decision Tree**

x[1]

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**x[1]** ©2015-2016 Emily Fox & Carlos Guestrin

x[1]

# Summary of decision trees

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# What you can do now

- Define a decision tree classifier
- Interpret the output of a decision trees
- Learn a decision tree classifier using greedy algorithm
- Traverse a decision tree to make predictions
  - Majority class predictions
  - Probability predictions
  - Multiclass classification

## Thank you to Dr. Krishna Sridhar



Dr. Krishna Sridhar Staff Data Scientist, Dato, Inc.

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