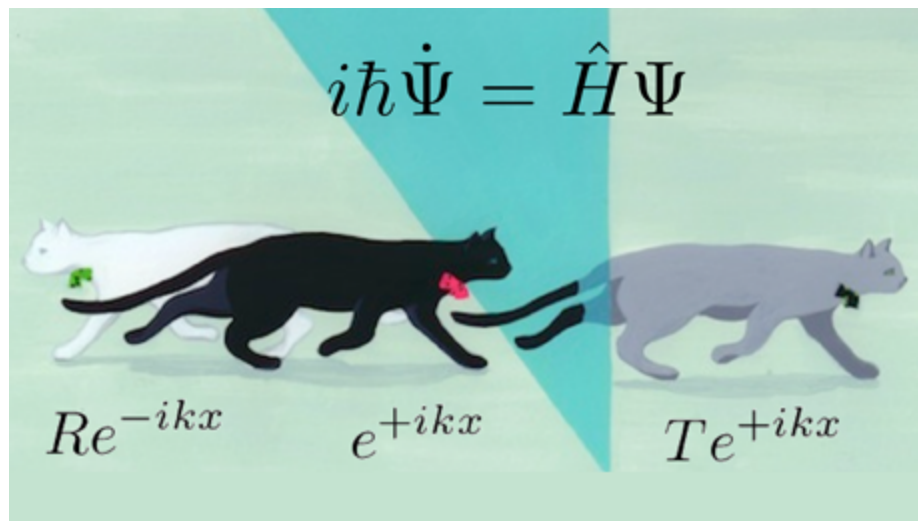


Symmetry in Quantum Physics

Part II. Parity and discrete symmetries



Symmetry in quantum physics

What constitutes a symmetry in quantum physics?

Suppose we have a solution to the Schrödinger equation

$$i\hbar \frac{\partial}{\partial t} \Psi = \hat{H} \Psi$$

And there is an operator which satisfies

$$[\hat{U}, \hat{H}] = \hat{U} \hat{H} - \hat{H} \hat{U} = 0$$

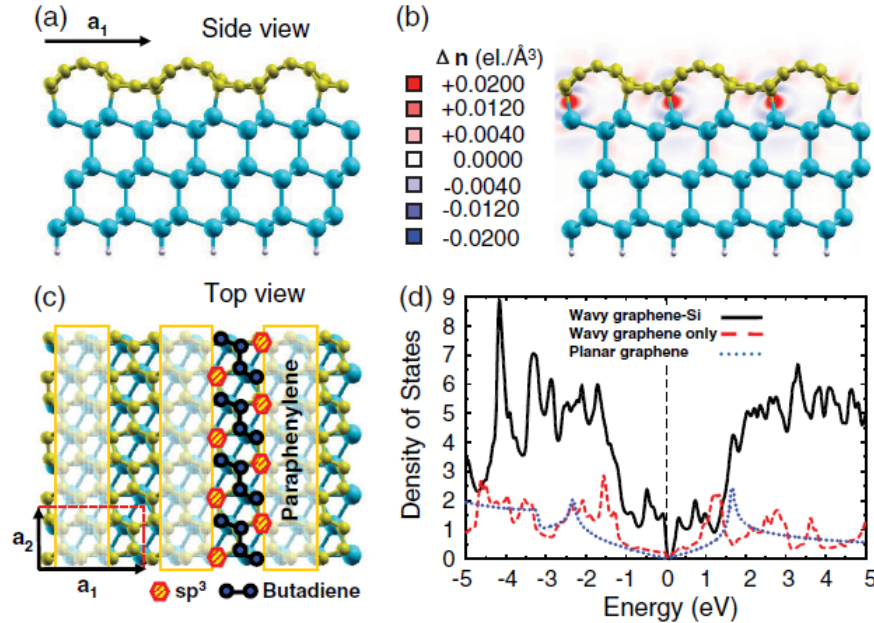
Then $i\hbar \frac{\partial}{\partial t} \hat{U} \Psi = \hat{H} \hat{U} \Psi$ so $\hat{U} \Psi$ is also a solution

We can require prospective solutions to be eigenfunctions of

$$\hat{U}$$

Symmetry in quantum physics

Why this is useful

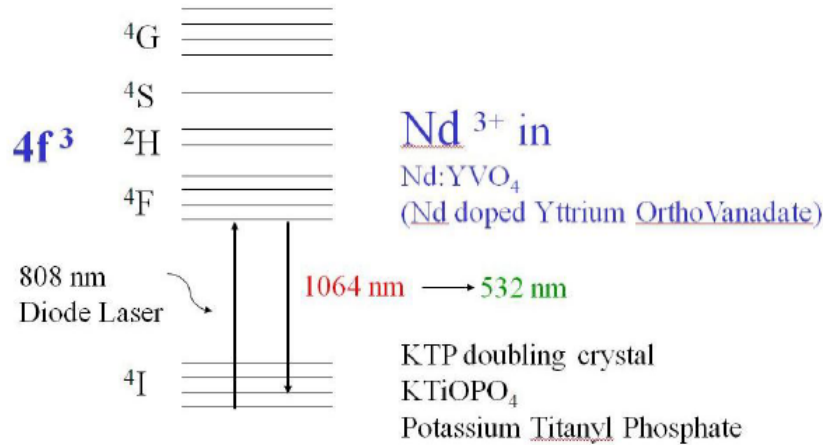


First-principles calculation of electronic structure of graphene, or interpreting its photoelectron spectrum or transport properties, is greatly simplified if one can treat one orbital symmetry at a time.

C. Tayran, et al. *PRL* **110**, 176805 (2013)

Symmetry in quantum physics

Why this is useful



I'm designing a laser system that needs to operate in a certain wavelength region. What optical sources are available, and which are the strongest transitions?

J. Galang, et al. , "The Green Laser Pointer"
in Exploring Quantum Physics Additional Materials

Symmetry in quantum physics

Simplest discrete symmetry: coordinate inversion (parity)

$$\hat{H} = \sum_{j=1}^N \left[\frac{\hat{p}_j^2}{2M_j} + \sum_{k \neq j}^N V_{jk} (|\vec{r}_j - \vec{r}_k|) \right]$$

A Hamiltonian describing many particles interacting via pairwise central interactions: quite a good approximation to many real materials.

Definition of parity operator $P\Psi(\vec{r}_1, \vec{r}_2, \dots, \vec{r}_n) = \Psi(-\vec{r}_1, -\vec{r}_2, \dots, -\vec{r}_n)$

$$[\hat{P}, \hat{H}] = 0 \quad ?$$

Symmetry in quantum physics

Simplest discrete symmetry: coordinate inversion (parity)

The particles in the previous example have charges q_j , and we turn on an electric field, \vec{E} .

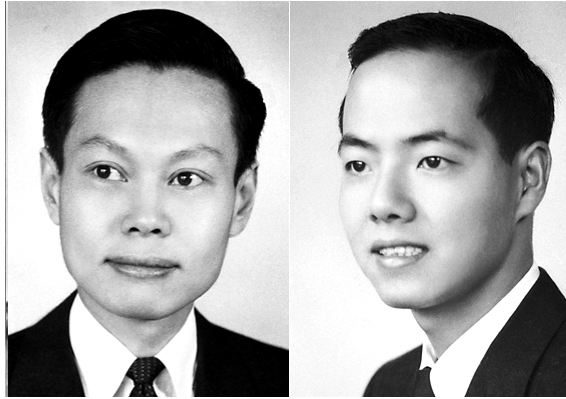
$$\hat{H} = \sum_{j=1}^N \left[\frac{\hat{p}_j^2}{2M_j} - q_j \vec{E} \cdot \vec{r}_j + \sum_{k \neq j}^N V_{jk} (|\vec{r}_j - \vec{r}_k|) \right]$$

Definition of parity operator $P\Psi(\vec{r}_1, \vec{r}_2, \dots, \vec{r}_n) = \Psi(-\vec{r}_1, -\vec{r}_2, \dots, -\vec{r}_n)$

$$[\hat{P}, \hat{H}] = 0 \quad ?$$

Symmetry in quantum physics

nobel.se public domain



Chen Ning Yang Tsung Dao Lee
1922- 1926-

1957 Nobel Prize in Physics

“for their penetrating investigation of the so-called parity laws which has led to important discoveries regarding the elementary particles”.

Parity

A towering symmetry in atomic, molecular, optical, condensed matter, nuclear and particle physics.

It is maximally violated in weak interactions!

The photon, an odd-parity particle, is now understood to be partnered with the W and Z bosons in the “electroweak theory”

Symmetry in quantum physics

Parity violation observed at the National Bureau of Standards, 1956

NIST

