

Fundamentals of Electrical Engineering Computation on a Computer

- Positional representation of numbers
- Base-2 numbers and powers of two

Number Representation

- One of the critical discoveries of mathematics was *positional notation*

$$257_{10} \text{ means } 2 \times 10^2 + 5 \times 10^1 + 7 \times 10^0$$

$$257_{10} = \text{CCLVII}$$

- In a computer, numbers are represented in *binary* (base 2)

$$100000001_2 \text{ means } 1 \times 2^8 + 0 \times 2^7 + 0 \times 2^6 + 0 \times 2^5 \\ + 0 \times 2^4 + 0 \times 2^3 + 0 \times 2^2 + 0 \times 2^1 + 1 \times 2^0$$

- Since $2^8 = 256$, $100000001_2 = 257_{10}$

Powers of Two

$$2^0 \quad 1$$

$$2^1 \quad 2$$

$$2^2 \quad 4$$

$$2^3 \quad 8$$

$$2^4 \quad 16$$

$$2^5 \quad 32$$

$$2^6 \quad 64$$

$$2^7 \quad 128$$

$$2^8 \quad 256$$

$$2^9 \quad 512$$

$$2^{10} \quad 1024$$

Computer Representation of Numbers

d ₇	d ₆	d ₅	d ₄	d ₃	d ₂	d ₁	d ₀
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unsigned 8-bit integer

0–255

s	d ₆	d ₅	d ₄	d ₃	d ₂	d ₁	d ₀
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signed 8-bit integer

-128–127

s		s	
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exponent

mantissa

floating point

$$m2^e, \frac{1}{2} \leq |m| < 1$$

Computer Representation of Numbers

- Numbers—signal values—are represented in a variety of ways, but always with discrete values
- Numbers are stored in individual memory locations
- Analog signals must be converted to digital signals for computer-based processing