

Design and Analysis of Algorithms I

### QuickSort

# Choosing a Good Pivot

#### QuickSort: High-Level Description

[Hoore circa 1961]

arckSat (array A, length n)

- -.4 N=1 VEFOLM
- p = Choo Se Rivot (A,n)
- Partition A around p
- recursively sat 1st part
- recursively sat 2nd part

[convertly unimplemented]

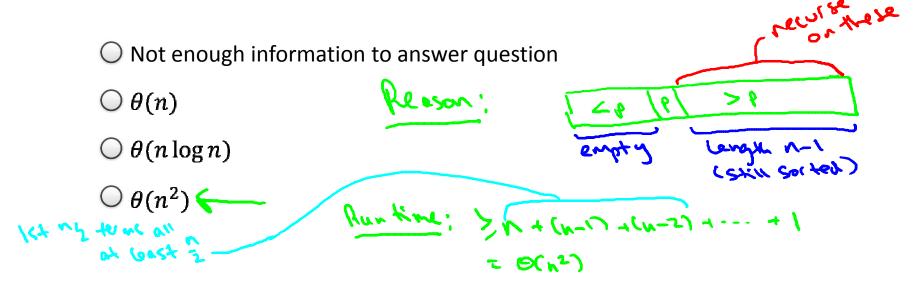
1st part 2nd part

#### The Importance of the Pivot

Q: lunning time et QuickSort?

A: depends on the quality of the pivot.

Suppose we implement QuickSort so that ChoosePivot always selects the first element of the array. What is the running time of this algorithm on an input array that is already sorted?



Suppose we run QuickSort on some input, and, magically, every recursive call chooses the median element of its subarray as its pivot. What's the running time in this case?

Not enough information to answer question

 $\bigcirc \theta(n)$ 

 $\theta(n\log n)$ 

 $\bigcirc \theta(n^2)$ 

Reason: let T(w) = running the m arrays of Size n. because push = median Then: T(n) = 2T(n) + O(n) => T(n) = O(n log n) [We marge Sort]

#### **Random Pivots**

Vey questin: houte choose pluts? Mc MEA: Nust S! That is: every recursive call, choose the pivot randomly.

(each elevent equally litely) Uge: a random privat is "pretty good" " often enough". Intrition! if always get a 25-75 golf 1900 evough for The Control of the Proce via recursion tree? Dhalf of elements give a 25-75 split or bother Q: does this reall y wolk?

## Average Running Time of QuickSort

Dicksat Theorem: for every input array of length in,

The average running the of Quicksat Cush random pivots)

The Otic login.

Mare: holds for every input. Eno assumptions on the data)

- real our guiding principles!
- "average" is over roudon choices made by the algorithm
  (i.e., plut choices)