



Design and Analysis  
of Algorithms I

# Introduction

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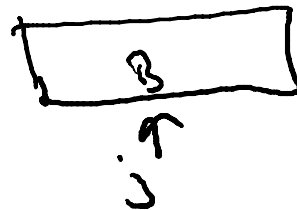
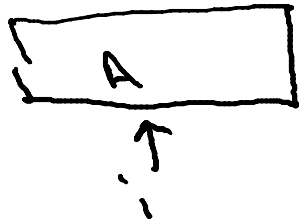
## Merge Sort (Pseudocode)

# Merge Sort: Pseudocode

- recursively sort 1st half of input array
  - "               " 2nd       "       "       "       "
  - merge two sorted sublists into one
- [ignores base cases]

## Pseudocode for Merge:

$C = \text{output array [length} = n]$   
 $A = \text{1st sorted array [} n/2]$   
 $B = \text{2nd " " [} n/2]$



$i = 1$   
 $j = 1$

for  $k = 1$  to  $n$   
  if  $A(i) < B(j)$   
     $C(k) = A(i)$   
     $i++$   
  else  $[B(j) < A(i)]$   
     $C(k) = B(j)$   
     $j++$

end *[ignore end cases]*

## Pseudocode for Merge:

C = output [length = n]

A = 1<sup>st</sup> sorted array [n/2]

B = 2<sup>nd</sup> sorted array [n/2]

i = 1

j = 1

for k = 1 to n

    if A(i) < B(j)

        C(k) = A(i)

        i++

    else [B(j) < A(i)]

        C(k) = B(j)

        j++

end

(ignores end cases)

# Merge Sort Running Time?

Key Question: running time of Merge Sort on  
array of  $n$  numbers?

Running time  $\approx$  # of lines of  
code executed

## Pseudocode for Merge:

C = output [length = n]

A = 1<sup>st</sup> sorted array [n/2]

B = 2<sup>nd</sup> sorted array [n/2]

i = 1

j = 1

*2 operations*

for k = 1 to n ✓

if A(i) < B(j) ✓

C(k) = A(i) —

i++ —

else [B(j) < A(i)]

C(k) = B(j) —

j++ —

end

(ignores end cases)

# Running Time of Merge

Upshot: running time of Merge on a array  
of  $m$  numbers is  $\leq 4m + 2$   
 $\leq 6m$  (since  $m \geq 1$ )

# Running Time of Merge Sort

Claim: Merge Sort requires

$\leq 6n \log_2 n + 6n$  operations  
to sort  $n$  numbers.

Recall:  $\log_2 n =$   
# of times you divide  
by 2 until you get  
down to 1.

