Quantum Mechanics & Quantum Computation

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Lecture 5: Quantum Gates

Taking Stock

Organizing Principles

• Kanban approach to math formalism.

($\alpha_0 | o \rangle + \alpha_1 | 1 \rangle$) ($\beta_0 | o \rangle + \beta_1 | 1 \rangle$) = $\alpha_0 \beta_0 | o 0 \rangle + \alpha_0 \beta_1 | o i \rangle + \cdots$ Measurements - operator

• Emphasize counter-intuitive aspects of QM.

Survey

- Level of lectures easy/hard?
- In-video quizzes are they helpful? Easier/harder?
- Level of homework questions easy/hard?
- Did you attempt the optional assignments? Would you like more optional questions?
- Linear algebra preparation do you want a review?
- Would you like to see some discussion of how some of the lecture topics relate to current research questions?

Bell's Experiment Setup



- Two boxes are very far apart.
- If both inputs are 1, want output bits to be different
 Otherwise, want outputs of the two boxes to be the same.

Boxes described by local hidden variables \rightarrow succeed with prob $\leq \frac{3}{4} = .75$ Boxes share a Bell state \rightarrow can succeed with prob as high as .85

Certifying Randomness

 Construct a physical random generator whose output can be certified to be random.



• Can use the Bell experiment to certify quantum randomness:

Succeed with probability close to $85\% \rightarrow a$, b random bits!

http://arxiv.org/pdf/0911.3427v3.pdf

http://arxiv.org/pdf/1111.6054v1.pdf